

# **Comorbidity Models**

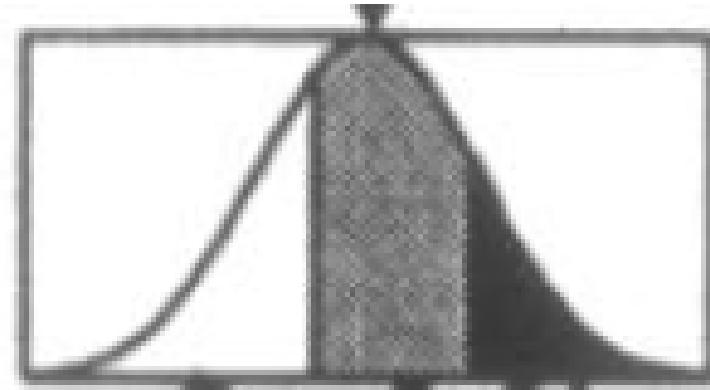
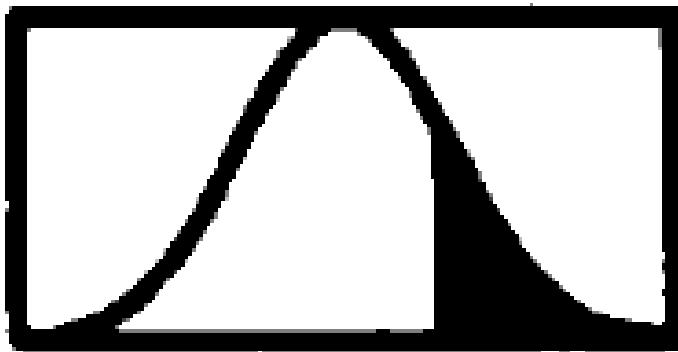
NIDA Advanced Genetic  
Epidemiology Workshop

# Introduction

- Substance use and disorders diagnosis is highly comorbid with other psychiatric disorders, such as depression, schizophrenia.
- Questions: are the two disorders distinct or do they reflect an arbitrary division of a single syndrome?

# Threshold model for liability

- Disease liability arises from the independent action of a large number of factors, each of small effect, which give rise to a normal distribution of liability. In the basic threshold model, individuals above an abrupt threshold have the disorder, whereas those below do not.



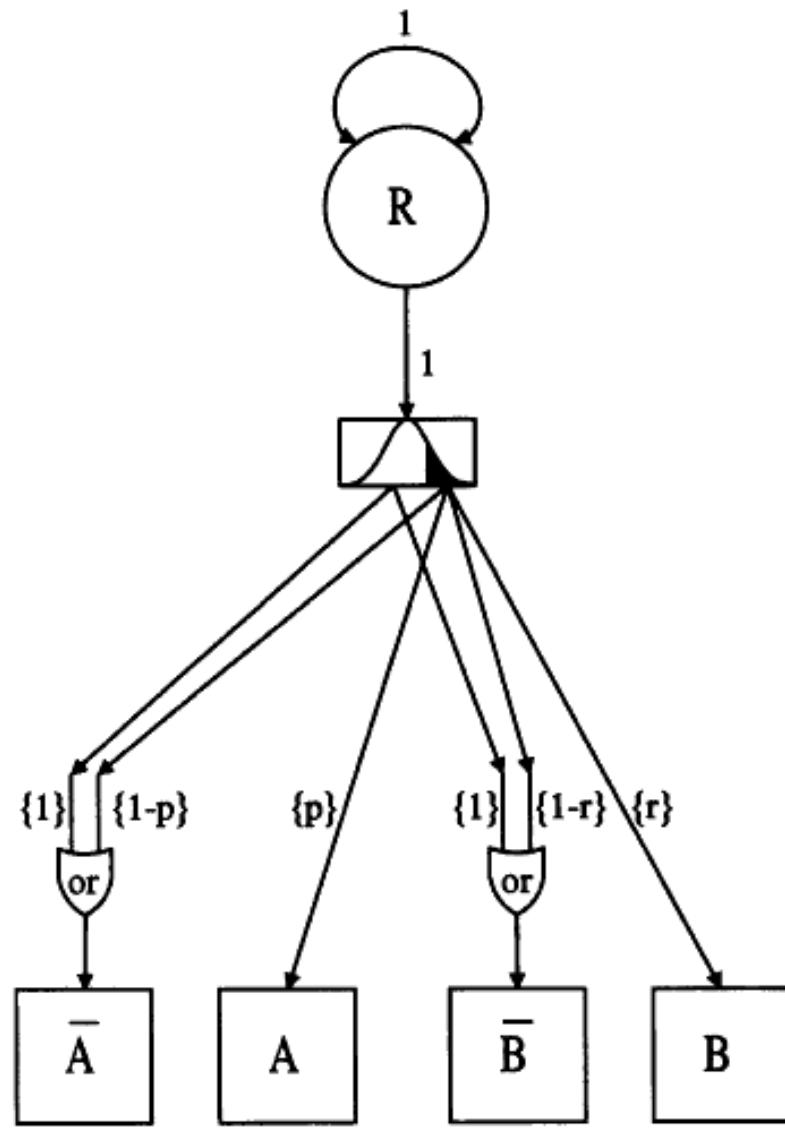
# Model 1. Alternate Forms

$$P(\bar{A}, \bar{B}) = L + (1 - p)(1 - r)U$$

$$P(\bar{A}, B) = p(1 - r)U$$

$$P(A, \bar{B}) = (1 - p)rU$$

$$P(A, B) = prU ,$$



R - Risk factors  
A - Disease A



- Threshold Filtration process

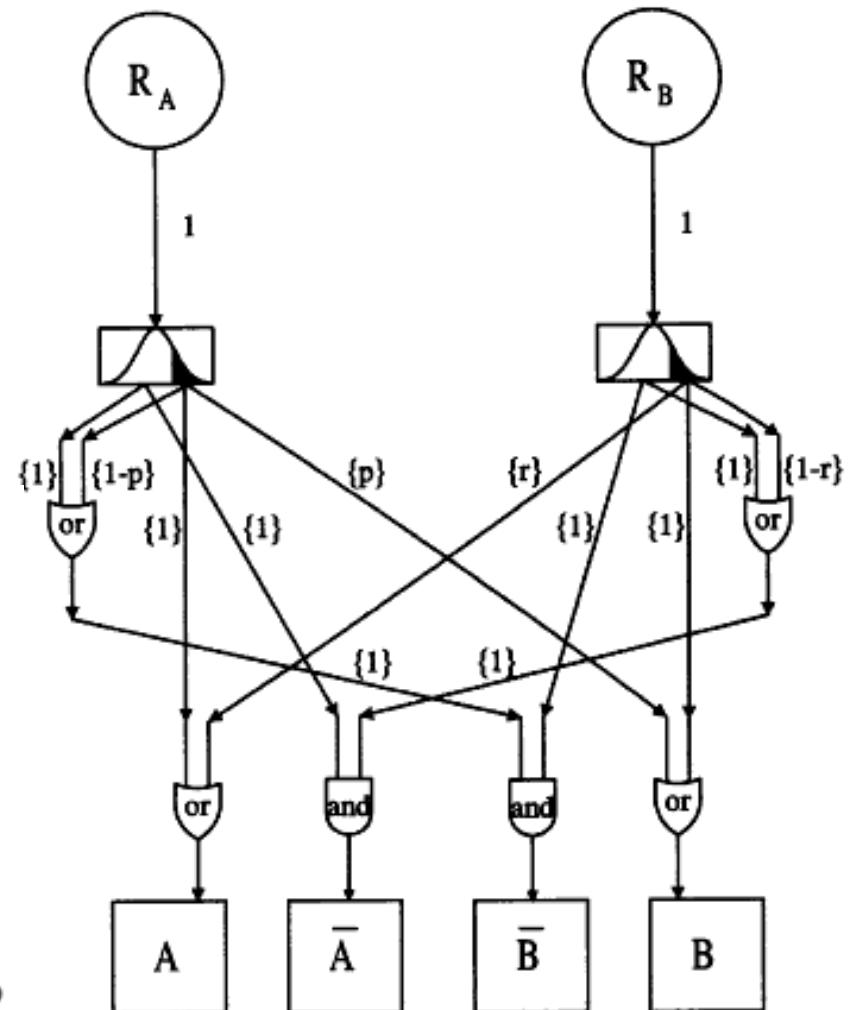
# Model 2. Random Multiformity

$$P(\bar{A}, \bar{B}) = L_A \cdot L_B$$

$$P(\bar{A}, B) = (1 - r)L_A \cdot U_B$$

$$P(A, \bar{B}) = U_A \cdot (1 - p)L_B$$

$$P(A, B) = U_A \cdot (U_B + pL_B) + rL_A \cdot U_B ,$$



R - Risk factors

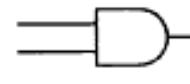
A - Disease A



. Threshold Filtration process



Or operation: A arises when LA or with probability r if LB is above threshold



And operation: not A arises when LA is below threshold and LB are above threshold

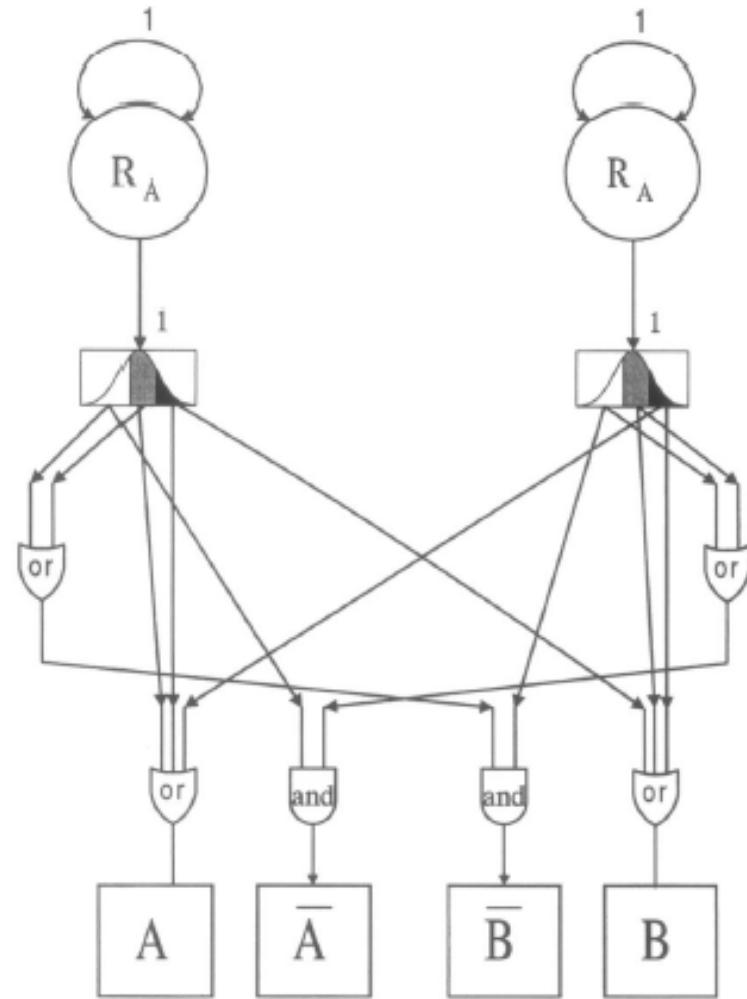
# Model 3. Extreme Multiformity

$$P(\bar{A}, \bar{B}) = L_A \cdot L_B$$

$$P(\bar{A}, B) = L_A \cdot M_B$$

$$P(A, \bar{B}) = M_A \cdot L_B$$

$$P(A, B) = U_A + U_B - U_A \cdot U_B + M_A \cdot M_B$$



R - Risk factors

A - Disease A



- Threshold Filtration process



Or operation: A arises when LA is above threshold 1 or if LB is above threshold 2



And operation: not A arises when LA is below threshold 1 and LB is below threshold 2

# Model 4.

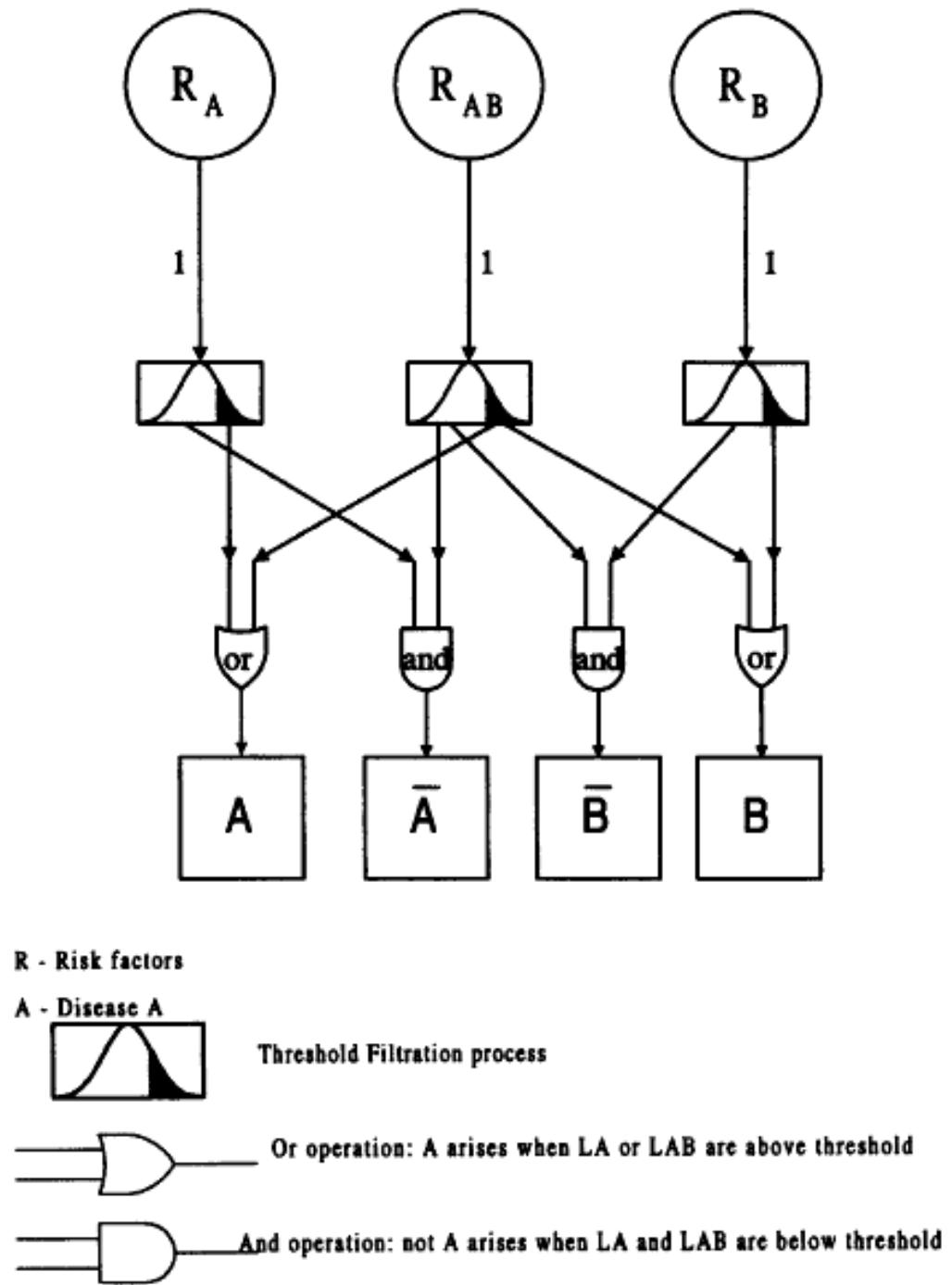
## Three independent

$$P(\bar{A}, \bar{B}) = L_A \cdot L_{AB} \cdot L_B$$

$$P(\bar{A}, B) = L_A \cdot L_{AB} \cdot U_B$$

$$P(A, \bar{B}) = U_A \cdot L_{AB} \cdot L_B$$

$$P(A, B) = U_A \cdot L_{AB} \cdot U_B + U_{AB}$$



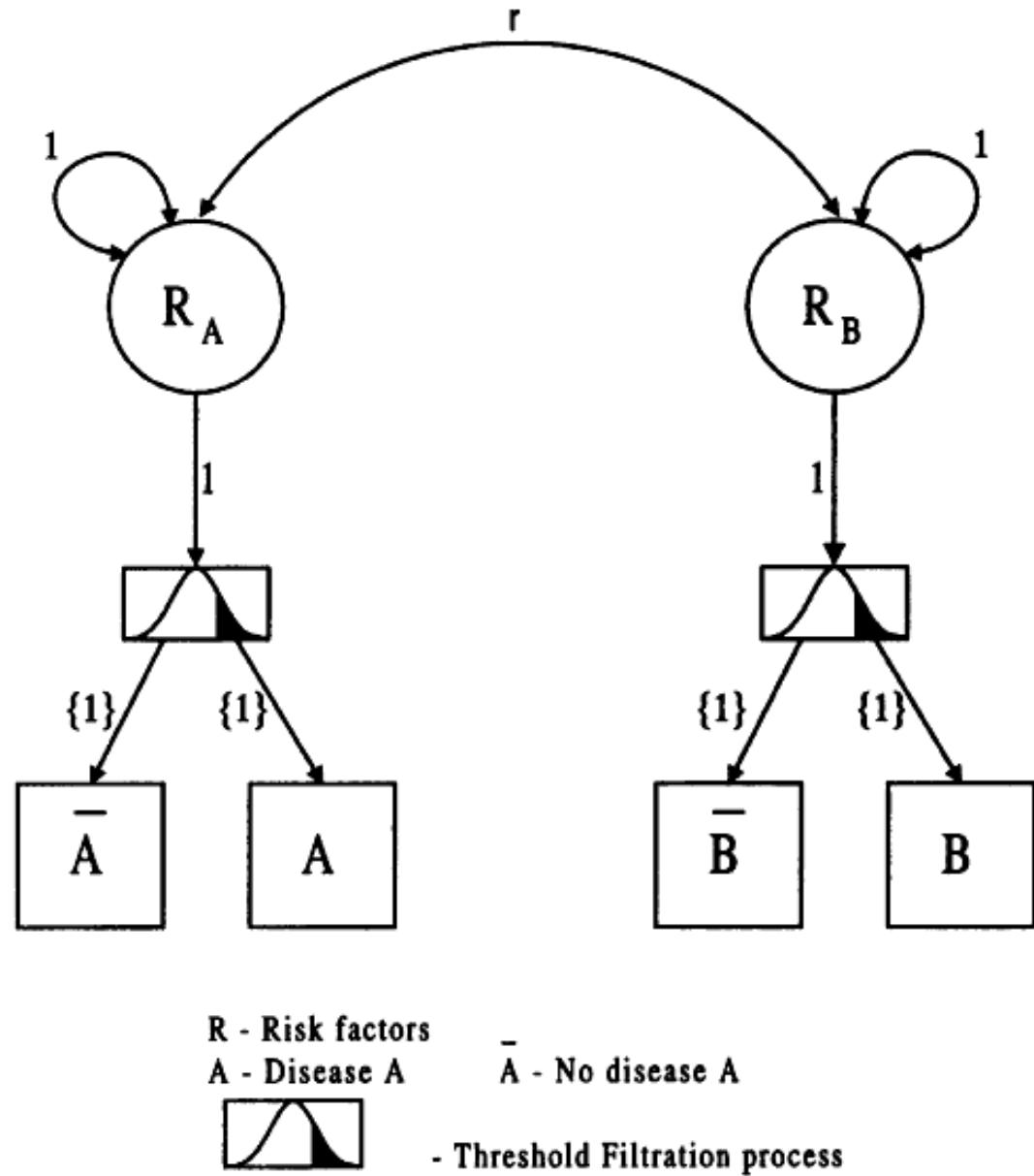
# Model 4. Correlated Liability

$$P(\bar{A}, \bar{B}) = LL_{A,B}$$

$$P(\bar{A}, B) = LU_{A,B}$$

$$P(A, \bar{B}) = UL_{A,B}$$

$$P(A, B) = UU_{A,B}$$



# Data Tabulation

		Twin 2		No		Yes	
		No	Yes	No	Yes	No	Yes
		No	----	---+	--+-	--++	
No	Yes	No	-+--	-+-+	-++-	-+++	
	Yes	No	+---	+--+	+-.+	+-.++	
Yes	Yes	No	++--	++-+	+++-	++++	

# 10 Flavors: Sum across Diagonal

		Twin 2		No		Yes		
		Twin 1	No	Yes	No	Yes		
No	No	----	---+	--+-	--++	-+-+	---	
	Yes		-+-+	-++-	-+++			
Yes	No			+--.	+--+.			
	Yes				++++			

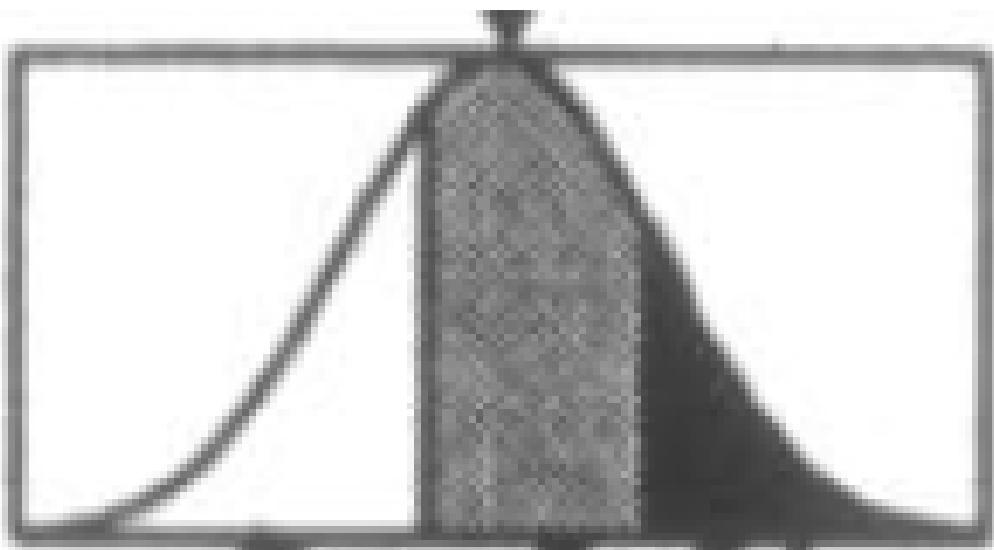
Legend:

- 
- +
- +-
- ++
- +-+
- ++-
- +++
- +--.
- +--+.
- ++++

**Observed Frequencies for Pairwise Diagnostic Data on MD and  
in MZ and DZ Female Twins**

		TWIN 1			
		No MD		MD	
TWIN 2		No GAD	GAD	No GAD	GAD
A. MZ Twins					
No MD	No GAD .....	282	25	54	29
No MD	GAD .....	19	3	3	9
MD	No GAD .....	31	10	8	18
MD	GAD .....	36	6	9	28
B. DZ Twins					
No MD	No GAD .....	155	20	38	34
No MD	GAD .....	22	4	1	9
MD	No GAD .....	38	8	11	13
MD	GAD .....	42	6	21	18

	<b>Twin 1</b>	<b>Twin2</b>
$LL_A$	<b>L</b>	<b>L</b>
$LM_A$	<b>L</b>	<b>M</b>
$LU_A$	<b>L</b>	<b>U</b>
$MM_A$	<b>M</b>	<b>M</b>
$MU_A$	<b>M</b>	<b>U</b>
$UU_A$	<b>U</b>	<b>U</b>



**L      M      U**

# Model 1.

## Alternate Forms

$$P(\bar{A}1, \bar{B}1, \bar{A}2, \bar{B}2) = LL + 2(1 - p)(1 - r)UL \\ + (1 - p)^2(1 - r)^2UU$$

$$P(\bar{A}1, \bar{B}1, \bar{A}2, B2) = r(1 - p)LU \\ + (1 - p)^2r(1 - r)^2UU$$

$$P(\bar{A}1, \bar{B}1, A2, \bar{B}2) = p(1 - r)LU \\ + p(1 - p)(1 - r)^2UU$$

$$P(\bar{A}1, \bar{B}1, A2, B2) = prLU \\ + p(1 - p)r(1 - r)UU$$

$$P(\bar{A}1, B1, \bar{A}2, B2) = (1 - p)^2r^2UU$$

$$P(\bar{A}1, B1, A2, \bar{B}2) = p(1 - p)r(1 - r)UU$$

$$P(\bar{A}1, B1, A2, B2) = p(1 - p)r^2UU$$

$$P(A1, \bar{B}1, A2, \bar{B}2) = p^2(1 - r)^2UU$$

$$P(A1, \bar{B}1, A2, B2) = p^2r(1 - r)UU$$

$$P(A1, B1, A2, B2) = p^2r^2UU .$$

# Model fitting

$$F = \sum_{i=1}^{10} \frac{(O_i - E_i)^2}{E_i}$$

**Fit Statistics Obtained for Various Models of Comorbidity  
Applied to Data on GAD and MD in Adult Female Twins**

MODEL NUMBER AND NAME	FIT STATISTIC			
	$\chi^2$	df	p	AIC
1 (Chance) .....	412.54	12	.00	388.54
2 (Alternate forms) .....	23.74	13	.03	-2.26
3 (Random multiformity) .....	25.59	10	.04	5.59
4 (Random multiformity of MD) .....	26.19	11	.06	4.19
5 (Random multiformity of GAD) .....	40.89	11	.00	18.89
6 (Extreme multiformity) .....	16.51	10	.08	-3.49
7 (Extreme multiformity of MD) .....	21.76	11	.03	-.24
8 (Extreme multiformity of GAD) .....	37.02	11	.00	15.02
9 (Three independent disorders) .....	39.77	9	.00	21.77
10 (Correlated liabilities) .....	12.23	9	.20	-5.77
11 (MD causes GAD) .....	14.79	11	.19	-7.21
12 (GAD causes MD) .....	21.09	11	.03	-.91
13 (Reciprocal causation) .....	12.29	10	.27	-7.71